

A analysis of 2^3 factorial design:

The sum of squares due to any factorial effect, main or interaction is obtained on multiplying the squares of the factorial effects total by 1 divided by $8 \cdot r$, where r is the common replication number. Thus for example,

$$\text{Sum of squares due to main effect } A = \frac{3^2}{8 \cdot r}, 1 \text{ d.f.}$$

$$\text{Sum of squares due to interaction effect } BC = \frac{3^2}{8 \cdot r}, 1 \text{ d.f.}$$

and so on.

These sums of squares are calculated from yate's table.

Yates's table for calculating treatment sum of squares:

Treatment Combination	Treatment Total	[1]	[2]	[3]	S.S = $\frac{[3]^2}{2^3 \cdot r}$
I	[I] = ①	①+② = ⑨	⑨+⑩ = ⑰	⑰+⑱ = ⑳	-
A	[A] = ②	③+④ = ⑩	⑪+⑫ = ⑱	⑲+⑳ = ㉔	$\frac{26^2}{8 \cdot r}$
B	[B] = ③	⑤+⑥ = ⑪	⑬+⑭ = ⑲	⑳+㉑ = ㉒	$\frac{27^2}{8 \cdot r}$
AB	[AB] = ④	⑦+⑧ = ⑫	⑮+⑯ = ㉒	㉓+㉔ = ㉖	$\frac{28^2}{8 \cdot r}$
C	[C] = ⑤	②-① = ⑬	⑩-⑨ = ⑲	⑱+⑰ = ㉒	$\frac{29^2}{8 \cdot r}$
Ac	[Ac] = ⑥	④-③ = ⑭	⑫-⑪ = ⑲	⑲+⑱ = ㉒	$\frac{30^2}{8 \cdot r}$
Bc	[Bc] = ⑦	⑥-⑤ = ⑮	⑭-⑬ = ⑲	⑲+⑱ = ㉒	$\frac{31^2}{8 \cdot r}$
ABC	[ABC] = ⑧	⑧-⑦ = ⑮	⑮-⑮ = ⑲	⑲+⑱ = ㉒	$\frac{32^2}{8 \cdot r}$

ANOVA Table :

S.V	d.f	S.S	M.S.S	F-R	F-T
Blocks (replication)	$(r-1)$	R.S.S	$a = \frac{R.S.S}{r-1}$	a/i	$F_{r-1, (r-1)(t-1)}$ df
Treatments					
A	1	S.S _A	$b = \frac{S.S_A}{1}$	b/i	$F_{1, (r-1)(t-1)}$ df
B	1	S.S _B	$c = S.S_B/1$	c/i	"
AB	1	S.S _{AB}	$d = S.S_{AB}/1$	d/i	"
C	1	S.S _C	$e = S.S_C/1$	e/i	"
AC	1	S.S _{AC}	$f = S.S_{AC}/1$	f/i	"
BC	1	S.S _{BC}	$g = S.S_{BC}/1$	g/i	"
ABC	1	S.S _{ABC}	$h = S.S_{ABC}/1$	h/i	"
Error	$(r-1)(t-1)$	S.S.E	$i = \frac{S.S.E}{(r-1)(t-1)}$		
Total	$(n-1)$	T.S.S			

Inference :

If the calculated value is less than the table value, null hypothesis is accepted. Otherwise it is rejected.